

# Intermediate Logic Spring

## Lecture Four

# Linguistic Ersatzism

Rob Trueman  
rob.trueman@york.ac.uk

University of York

# Linguistic Ersatzism

## Introduction

Defining Linguistic Ersatzism

Primitive Modality

A Lagadonian Language

The Problem of Alien Properties

## Re-Cap: Genuine Modal Realism

- According to Lewis' **genuine modal realism**, other possible worlds are just as real as the actual world
  - There are possible worlds which contain talking donkeys, and those possible talking donkeys are just as real and flesh-and-blood as the actual mute donkeys
- **Official Definition:** A possible world is a maximal spatiotemporal sum
- Lewis argues for genuine modal realism via a **cost-benefit analysis**
  - The commitment to real possible worlds is an *ontological cost* of the theory, but Lewis insists that that cost is offset by many many *benefits*

## How to Reply to Lewis

- (1) Argue that the whole idea of real possible worlds *is* incoherent, after all
  - We looked at some arguments of this type in the last seminar
- (2) Argue that genuine modal realism doesn't deliver all of the benefits it promises
  - We briefly looked at one argument along these lines last week
- (3) Argue that we can get all of the benefits that genuine modal realism offers *without* positing real possible worlds
  - This is the strategy we will pursue this week

## Introducing Ersatz Modal Realism

- In this lecture, we will be looking at **ersatz modal realism** (or *ersatzism* for short)
- According to ersatz realism, possible worlds do exist, but they are not the concrete, maximal spatiotemporal sums that Lewis believes in
- Instead, they are *ersatz worlds*, which do the work of Lewis' real possible worlds without the metaphysical extravagance
  - The adjective 'ersatz' means: made or used as a substitute, typically an inferior one, for something else: e.g. ersatz coffee

## Three Varieties of Ersatzism

- Ersatzism comes in a number of different varieties
- Different varieties of ersatzism put forward different entities to serve as the ersatz worlds
- Lewis distinguishes between three different varieties in Chapter 3 of *On the Plurality of Worlds*
  - **Linguistic ersatzism**
  - **Pictorial ersatzism**
  - **Magical ersatzism**
- In this lecture, we will focus on just one variety: **linguistic ersatzism**

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## Possible Worlds are Stories

- **A natural thought:** Possible worlds are a kind of *story*
- Possible talking donkeys are not real, flesh-and-blood donkeys living in another real world
- When we say that there is a possible world in which donkeys talk, all we are saying is that there is a *story* according to which donkeys talk
- Talking donkeys are nothing but characters in fictional stories





## Worlds as Sets of Sentences

- Possible worlds cannot be stories in quite the everyday sense
- In the everyday sense, stories don't exist until someone actually sits down and writes them out
- But we don't want the existence of a possible world in which donkeys talk to depend on whether anyone has ever actually written a story which stars a talking donkey
- Instead, we should think of possible worlds as **sets of sentences**
- Whether or not anyone has ever told a story about talking donkeys, there will certainly be a set containing the sentence 'There is a talking donkey'

## Worlds as Consistent Sets of Sentences

- Not every **set of sentences** gets to count as a world
- Some sets of sentences are **inconsistent**, meaning that the sentences in that set could not all be true together

{‘There is a talking donkey’, ‘No donkey talks’}

- So, we should really think of possible worlds as **consistent sets of sentences**

## An Incompleteness Problem

- Not every **consistent set of sentences** gets to count as a world
- Consider the following consistent set:  
 $\{\text{'There is a talking donkey'}\}$
- This set can't really count as a possible world, because it is incomplete
  - It tells us hardly anything about what happens at that world
- To get a full-fledge possible world, we need to add details about **everything** which happens at that world

## Worlds as Maximally Consistent Sets of Sentences

- Instead, possible worlds are **maximally consistent sets of sentences**
- A set,  $w$ , is maximally consistent iff it meets the following two conditions:
  - (i)  $w$  is consistent
  - (ii) For any set of sentences  $w'$ , if  $w$  is a proper subset of  $w'$ , then  $w'$  is inconsistent
- **Put more intuitively:**
  - $w$  is maximally consistent iff  $w$  is consistent, and we could not add any more sentences to  $w$  without making it inconsistent
- In other words, possible worlds are sets of sentences which are as detailed as they consistently can be

## Linguistic Ersatzism

- **Linguistic ersatzism** is the thesis that possible worlds are maximally consistent sets of sentences
- For linguistic ersatzism, the fundamental notion of truth **is not** relativised to a world
  - Fundamentally, sentences are true or false *full stop*, not true or false *relative to a world*
- Linguistic ersatzism defines **truth at a world** as follows:
  - Sentence  $s$  is *true at world  $w$*  iff the members of  $w$  jointly entail  $s$
- Linguistic ersatzism defines **the actual world** as follows:
  - A maximally consistent set of sentences,  $w$ , is the *actual world* iff every member of  $w$  is true

## Linguistic Ersatzism versus Genuine Modal Realism

- Compared to genuine modal realism, linguistic ersatzism appears to have a safe and sensible ontology
  - We all believe in sentences already, and mathematicians appeal to sets all of the time
  - So linguistic ersatzism builds its possible worlds out of things we already believed in
- Unfortunately, in Chapter 3 of *Plurality*, Lewis argues that linguistic ersatzism doesn't deliver as many benefits as genuine modal realism. . .

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## Analysing Modality

- Lewis claims that one of the great benefits of genuine modal realism is that it allows us to give a non-modal analysis of *possibility*
  - $\diamond P$  iff there is some maximal spatiotemporal sum at which  $P$
- As we saw last week, it's not *entirely* obvious that Lewis is right about this. . .
- But whether or not Lewis really gives us a non-modal analysis of *possibility*, he is keen to emphasise that linguistic ersatzism **definitely doesn't**



## What does 'Consistent' Mean?

- **Linguistic Ersatzism:** possible worlds are maximally *consistent* sets of sentences
- **What does 'consistent' mean?**
  - (1) A set of sentences is consistent iff all of the sentences in that set could be true together
  - (2) A set of sentences is consistent iff there is some possible world at which all of the sentences in that set are true
  - (3) A set of sentences is consistent iff there is some interpretation on which all of the sentences in that set are true
  - (4) A set of sentences is consistent iff there is no proof of a contradiction from the sentences in that set
- None of these options will let a linguistic ersatzer give a non-modal analysis of *consistency*

## Consistency as Modal

- (1) **A set of sentences is consistent iff all of the sentences in that set could be true together**
  - This is a *modal* definition of *consistency*
  - If a linguistic ersatzer uses this modal definition of *consistency*, then they will have given a modal definition of what they mean by 'possible world'
  - They can still define *possibility* in terms of worlds:
    - $\Diamond P$  iff ' $P$ ' is entailed by some maximally consistent set of sentences
  - But crucially, this will not be an analysis of *possibility* in **non-modal** terms

## Consistency as Truth at a World

- (2) **A set of sentences is consistent iff there is some possible world at which all of the sentences in that set are true**
- This definition of consistency is **useless** for a linguistic ersatzer
  - We are trying to think of possible worlds as maximally consistent sets of sentences, but then use talk of possible worlds to explain what we mean by 'consistent'
  - That looks like a pretty vicious circle!

## Consistency as Semantic

(3) **A set of sentences is consistent iff there is some interpretation on which all of the sentences in that set are true**

- On this definition, when we say that two sentences are consistent, we are saying that there is some way of **re-interpreting** them so that they are both true
  - ‘a is red’ and ‘a is green’ are consistent because we can interpret ‘is red’ to mean *is human* and ‘is green’ to mean *is an electrician*
- But when we ask whether there is a world in which something is both red and green, we don’t want to know if there is some way of **re-interpreting** ‘is red’ and ‘is green’ to make ‘a is red’ and ‘a is green’ both true!

## Consistency as Syntactic

- (4) **A set of sentences is consistent iff there is no proof of a contradiction from the sentences in that set**
- The trouble with this definition is that it sets the bar for consistency too low (for the purposes of linguistic ersatzism)
  - You cannot use the proof rules for FOL (or any other logic!) to derive a contradiction from this set:
    - {‘a is red all over’, ‘a is green all over’}
  - Nonetheless, you might think it is impossible for something to be red all over and green all over

## Adding Axioms?

- As Lewis acknowledges (*Plurality*, pp. 152–6), we could get around this problem by adding **axioms** to our logic
  - When we add axioms to the rules of FOL, we are allowed to appeal to them at any time in any proof
  - If we want to rule out worlds where something is red and green, just add as an axiom: *Nothing is red all over and green all over*
- The trouble is that we have no idea what axioms we should actually add
- We could get around this by simply stipulating that we should add an axiom just in case that axiom is **necessarily true**, but then we would have gone back to using modal concepts in our account of possible worlds

## A Weaker World-Making Language?

- The problem with (4) only comes up because our language is rich enough to include **atomic sentences** that are **impossible** (i.e. can't be true together)
- Maybe we could get around this problem by using a less rich **world-making language**?
- But if the world-making language is too poor, then the problem becomes explaining how sentences in the poor language can **entail** sentences in richer languages
- The old problems about consistency then re-appear as problems about entailment (see Lewis, *Plurality*, pp.151–2)

## No Non-Modal Analysis of Possibility

- **Four Definitions of 'Consistent'**

- (1) A set of sentences is consistent iff all of the sentences in that set could be true together
  - (2) A set of sentences is consistent iff there is some possible world at which all of the sentences in that set are true
  - (3) A set of sentences is consistent iff there is some interpretation on which all of the sentences in that set are true
  - (4) A set of sentences is consistent iff there is no proof of a contradiction from the sentences in that set
- If the linguistic ersatzer chooses (1), then she will be using modal concepts in her analysis of *possibility*



## No Non-Modal Analysis of Possibility

- **Four Definitions of 'Consistent'**
  - (1) A set of sentences is consistent iff all of the sentences in that set could be true together
  - (2) A set of sentences is consistent iff there is some possible world at which all of the sentences in that set are true
  - (3) A set of sentences is consistent iff there is some interpretation on which all of the sentences in that set are true
  - (4) A set of sentences is consistent iff there is no proof of a contradiction from the sentences in that set
- The linguistic ersatzer cannot choose (2) or (3) — they are inappropriate for her purposes

## No Non-Modal Analysis of Possibility

- **Four Definitions of 'Consistent'**
  - (1) A set of sentences is consistent iff all of the sentences in that set could be true together
  - (2) A set of sentences is consistent iff there is some possible world at which all of the sentences in that set are true
  - (3) A set of sentences is consistent iff there is some interpretation on which all of the sentences in that set are true
  - (4) A set of sentences is consistent iff there is no proof of a contradiction from the sentences in that set
- If the linguistic ersatzer chooses (4), then she will need to add all sorts of axioms, and we don't know how to specify which ones to add non-modally

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## What is the World-Making Language?

- For the linguistic ersatzer, possible worlds are maximally consistent sets of sentences
- **But sentences of which language!?**
- It won't do to use plain old English: there are lots of individuals we don't have names for in English, and lots of properties we don't have predicates for
  - English as it was 300 years ago didn't have the means to express the property of *being a smartphone*
  - It seems a safe bet that in 300 years time, people will look back on our language and say that there were certain properties we couldn't express!

## A Lagadonian Language

- It is clear that we will need to use a different kind of language to build the linguistic ersatzer's worlds
- Lewis (*Plurality*, pp. 145–6) suggests that we use a **Lagadonian** language
- In a Lagadonian language, we use each individual *as a name for itself*, and each property *as a predicate expressing itself*

## A Lagadonian Language

- The name comes from Jonathan Swift's *Gulliver's Travels*
- Gulliver meets some linguists in a city called Lagado, who are experimenting with a language in which everything is a name for itself
- This language has its advantages — it is universal — but it is also impractical
- People have to carry around huge sacks filled with everything they want to talk about, so they can pull them out in conversation when needed!



## A Set-Theoretic Lagadonian Language

- Lewis' version of a Lagadonian uses set-theory to eliminate the need to actually carry around the objects you want to talk about
- An (atomic) Lagadonian sentence is an **ordered sequence** of a property or relation, followed by the appropriate number of individuals
  - An **ordered sequence** is a lot like a set, except we keep track of the order of the members of a sequence
  - $\{\text{Frege, Wittgenstein}\} = \{\text{Wittgenstein, Frege}\}$ , because these sets have exactly the same members: Frege and Wittgenstein
  - $\langle \text{Frege, Wittgenstein} \rangle \neq \langle \text{Wittgenstein, Frege} \rangle$ , because although these sequences have the same members, they have them in different orders
  - $\langle a_1, \dots, a_n \rangle = \langle b_1, \dots, b_n \rangle \leftrightarrow (a_1 = b_1 \wedge \dots \wedge a_n = b_n)$

## A Set-Theoretic Lagadonian Language

- **Here is an example of a Lagadonian sentence:**
  - $\langle$ The property of *being human*, Socrates $\rangle$
- This Lagadonian sentence is the ordered sequence of a property, followed by an individual; it says that Socrates is human
- **Here is another example:**
  - $\langle$ The relation of *loving*, Antony, Cleopatra $\rangle$
- This Lagadonian sentence is the ordered sequence of a two-place relation, followed by two individuals; it says that Antony loves Cleopatra



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## Alien Properties

- We can use a Lagadonian language to construct a wealth of ersatz possible worlds
- **But there is a limit!**
- We can refer to any individual and any property in the *actual world*
- But couldn't there be **alien properties**, properties which are not actually instantiated, and which cannot be constructed out of properties which are instantiated?
- It is not at all clear how a linguistic ersatzer could accommodate the possibility of alien properties

## Alien Properties and Genuine Modal Realism

- Alien properties posed a problem for Lewis' attempt to use a **Recombination Principle** to generate all the real possible worlds he needs
- But importantly, Lewis *can* accommodate alien properties, so long as he is willing to use a modal principle in his account of what worlds there are, rather than Recombination
- Lewis (*Plurality* pp. 158–65) uses the fact that his theory can accommodate alien properties and linguistic ersatzism doesn't seem to be able to as an argument for his theory

## Two Strategies for Dealing with Alien Properties

- There are two ways that a linguistic ersatzer could deal with the problem of alien properties
  - (1) They could try to find some way of accounting for the possibility of alien properties within their theory
  - (2) They might simply *deny* that alien properties are really possible

## Don't Name, Describe!

- We can't **name** alien properties in a Lagadonian language, but we could still **describe** them
- Suppose you thought there could be a world where every atomic particle had some alien property
- You could put the following sentence into one of your maximally consistent sets of sentences:
  - There is some property,  $p$  such that every fundamental particle instantiates  $p$ , and  $p$  cannot be built out of ...  
(you fill in the dots with a long list of all the fundamental properties in the actual world)

## Conflating Distinct Possibilities

- Lewis considers this option in Chapter 3 of *Plurality*, but rejects it because he thinks it *conflates* distinct possibilities
- Imagine that  $w_1$  and  $w_2$  are exactly the same, except the fundamental particles in  $w_1$  have one alien property, and the fundamental particles in  $w_2$  have a *different* alien property
- There's no way for a linguistic ersatzer to distinguish these worlds
  - As far as the alien properties go, they both just say: 'There is some property,  $p$  such that every fundamental particle instantiates  $p$ , and  $p$  cannot be built out of ...'

## Two Possible Replies

- (1) Find a way for the linguistic ersatzer to distinguish between worlds like  $w_1$  and  $w_2$ 
  - Melia pursues this strategy in his *Modality*, pp. 160–72
  
- (2) Deny that the linguistic ersatzer needs to admit any distinction between  $w_1$  and  $w_2$ 
  - But if you are going to pursue this strategy, maybe you would be better off just denying that the linguistic ersatzer needs to admit the possibility of alien properties...

## Why Accept that Alien Properties are Possible?

- Imagine a world,  $w$ , in which there was no electromagnetic force
- From the point of view of  $w$ , *negative charge* is alien
- But if our world has properties that are alien to  $w$ , why shouldn't another world have properties which are alien to us?
- Why think that our world is so special that there couldn't be any properties alien to us?





## Denying the Possibility of Alien Properties

- This looks like a good argument *if you are a genuine modal realist*
  - According to genuine modal realism, there is nothing metaphysically special about the actual world
- But for the linguistic ersatzer, the actual world is **metaphysically privileged**
  - The actual world is the only maximally consistent set of sentences which only contains **true** sentences
- It may be, then, that the linguistic ersatzer could coherently deny that there could be properties which are not reducible to the properties instantiated at the actual world
- That is something I will leave you to think about!

## Seminar 4

- The reading for Seminar 4 is:
  - David Lewis, *On the Plurality of Worlds*, ch.3
- Access to this chapter is available via the Reading List on the VLE
- A number of study questions have been posted on the VLE; why not meet up and discuss them in groups?

## Lecture and Seminar 5

- Next week, we will start looking at **Second-Order Logic**
- Please make sure that you read the *Second-Order Logic Primer*, available on the VLE